Rotational Kinematics
Definitions:

Angular Position:

$$\theta$$

Angular Displacement:

$$\Delta\theta$$

Average Angular Velocity:

$$\bar{\omega}_z = \frac{\Delta\theta}{\Delta t}$$

Instantaneous Angular Velocity:

$$\omega_z = \lim_{\Delta t \to 0} \frac{\Delta\theta}{\Delta t} = \frac{d\theta}{dt}$$

Average Angular Acceleration:

$$\bar{\alpha}_z = \frac{\Delta\omega}{\Delta t}$$

Instantaneous Angular Acceleration:

$$\alpha_z \equiv \lim_{\Delta t \to 0} \frac{\Delta\omega}{\Delta t} = \frac{d\omega}{dt}$$

Kinematic Equations:

Rotational (Angular) Kinematics

$$\omega_f = \omega_i + \alpha\Delta t$$

$$\theta_f = \theta_i + \omega_i\Delta t + \frac{1}{2}\alpha(\Delta t)^2$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta$$

Linear Kinematics

$$v_f = v_i + a\,\Delta t$$

$$s_f = s_i + v_i\,\Delta t + \frac{1}{2}a\,(\Delta t)^2$$

$$v_f^2 = v_i^2 + 2a\,\Delta s$$

Linear-Angular Relationships:

Position:

$$s = r\,\theta$$

Speed:

$$\frac{ds}{dt} = r\frac{d\theta}{dt}$$

$$v_t = r\omega$$

Linear Acceleration

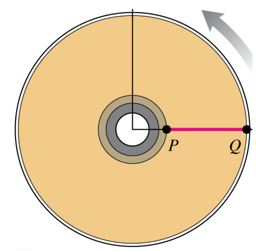
$$\frac{dv}{dt} = r\frac{d\omega}{dt}$$

$$a_t = r\alpha$$

Centripetal Acceleration

$$a_r = \frac{v^2}{r} = \omega^2 r$$

Constant Angular Acceleration: A Blu-ray disc is slowing to a stop. The disc's angular velocity at t = 0 is 27.5 rad/s, and its angular acceleration is a constant −10 rad/s^2. A line PQ on the disc's surface lies along the +x-axis at t = 0.



a. What is the disc's angular velocity at t = 0.300 s?

b. What angle does the line PQ make with the +x-axis at this time?